## EE881 - PRINCÍPIOS DE COMUNICAÇÕES - 1ª LISTA - Prof. Luís Meloni

## Exercícios de Análise de Fourier

1°)

Calcule e plote a transformada de Fourier para:

e) sgn(t) – função sinal

a) 
$$e^{-2(t-1)}u(t-1)$$
  
b)  $e^{-2|t-1|}$ 

b) 
$$e^{-2|t-1|}$$

c) 
$$\delta(t+1) + \delta(t-1)$$

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d)  $\frac{d}{dt}\{u(-2-t) + u(t-2)\}$ 

2°)

Considere o sinal abaixo:

$$x(t) = \begin{cases} 0, & t < -\frac{1}{2} \\ t + \frac{1}{2}, & -\frac{1}{2} \le t \le \frac{1}{2} \\ 1, & t > \frac{1}{2} \end{cases}$$

- a) Use as propriedades de integração e diferenciação para encontrar a transformada de Fourier de x(t).
- b) Qual é a transformada de Fourier de  $g(t) = x(t) \frac{1}{2}$
- 3°) Calcule a transformada de Fourier de cada um dos sinais abaixo.

a) 
$$[e^{-\alpha t}\cos\omega_0 t]u(t), \alpha > 0$$

a) 
$$[e^{-\alpha t} \cos \omega_0 t] u(t), \alpha > 0$$
  
b)  $x(t) = \begin{cases} 1 + \cos \pi t, & |t| \le 1 \\ 0, & |t| > 1 \end{cases}$ 

c) 
$$\sum_{k=0}^{\infty} \alpha^k \delta(t-kT)$$
,  $|\alpha| < 1$ 

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$$\sum_{k=0}^{\infty} \alpha^k \delta(t - kT)$$
,  $|\alpha| < 1$   
d) $x(t) = \begin{cases} 1 - t^2, & 0 < t < 1\\ 0, & c. c. \end{cases}$ 

e)x(t) como mostrado na figura 1.

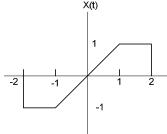


Figura 1

4°) Calcule a transforma de Fourier dos sinais discretos abaixo.

a) 
$$x[n]=u[n-2]-u[n-6]$$
  
b)  $x[n] = \left(\frac{1}{2}\right)^{-n} u[-n-1]$   
c)  $x[n] = \left(\frac{1}{2}\right)^{|n|} \cos(\frac{\pi}{8}(n-1))$   
d)  $x[n] = x[n-6] e x[n]=u[n]-u[n-5] para  $0 \le n \le 5$ .$ 

5°) Calcule a transforma de Fourier discreta inversa dos espectros abaixo.

$$a)X(e^{j\omega}) = \begin{cases} 1, \frac{\pi}{4} \le |\omega| \le \frac{3\pi}{4} \\ 0, \frac{3\pi}{4} \le |\omega| \le \pi, \ 0 \le |\omega| < \frac{\pi}{4} \end{cases}$$

$$b) X(e^{j\omega}) = 1 + 3e^{-j\omega} + 2e^{-j2\omega} - 4e^{-j3\omega} + e^{-j10\omega}$$

$$c)X(e^{j\omega}) = \frac{1 - \frac{1}{3}e^{j\omega}}{1 - \frac{1}{4}e^{-j\omega} - \frac{1}{8}e^{-2j\omega}}$$

## Exercícios selecionados do livro do Lathi, Modern Digital and Analog Communication Systems, 3rd Ed.

6°)

- **4.2-4** You are asked to design a DSB-SC modulator to generate a modulated signal  $km(t) \cos \omega_c t$ , where m(t) is a signal band-limited to B Hz. Figure P4.2-4 shows a DSB-SC modulator available in the stock room. The carrier generator available generates not  $\cos \omega_c t$ , but  $\cos^3 \omega_c t$ . Explain whether you would be able to generate the desired signal using only this equipment. You may use any kind of filter you like.
  - (a) What kind of filter is required in Fig. P4.2-4?
  - (b) Determine the signal spectra at points b and c, and indicate the frequency bands occupied by these spectra.
  - (c) What is the minimum usable value of  $\omega_c$ ?
  - (d) Would this scheme work if the carrier generator output were  $\cos^2 \omega_c t$ ? Explain.
  - (e) Would this scheme work if the carrier generator output were  $\cos^n \omega_c t$  for any integer  $n \ge 2$ ?

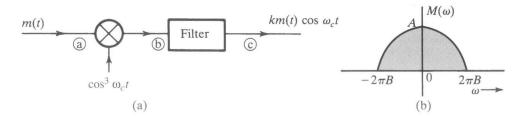


Figure P4.2-4

- **4.2-8** Two signals  $m_1(t)$  and  $m_2(t)$ , both band-limited to 5000 rad/s, are to be transmitted simultaneously over a channel by the multiplexing scheme shown in Fig. P4.2-8. The signal at point b is the multiplexed signal, which now modulates a carrier of frequency 20,000 rad/s. The modulated signal at point c is transmitted over a channel.
  - (a) Sketch signal spectra at points a, b, and c.
  - (b) What must be the bandwidth of the channel?
  - (c) Design a receiver to recover signals  $m_1(t)$  and  $m_2(t)$  from the modulated signal at point c.

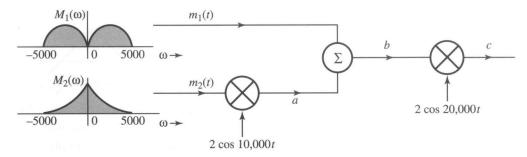


Figure P4.2-8

8°) e 9°)

**4.3-1** Figure P4.3-1 shows a scheme for coherent (synchronous) demodulation. Show that this scheme can demodulate the AM signal  $[A + m(t)] \cos \omega_c t$  regardless of the value of A.

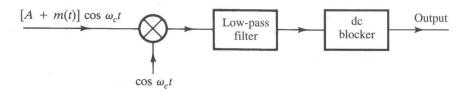


Figure P4.3-1

**4.3-2** Sketch the AM signal  $[A+m(t)]\cos \omega_c t$  for the periodic triangle signal m(t) shown in Fig. P4.3-2 corresponding to the modulation index: (a)  $\mu = 0.5$ ; (b)  $\mu = 1$ ; (c)  $\mu = 2$ ; (d)  $\mu = \infty$ . How do you interpret the case  $\mu = \infty$ ?

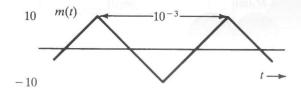


Figure P4.3-2

10°)

5.1-2 A baseband signal m(t) is the periodic sawtooth signal shown in Fig. P5.1-2. Sketch  $\varphi_{FM}(t)$  and  $\varphi_{PM}(t)$  for this signal m(t) if  $\omega_c = 2\pi \times 10^6$ ,  $k_f = 2000\pi$ , and  $k_p = \pi/2$ . Explain why it is necessary to use  $k_p < \pi$  in this case.

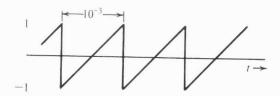


Figure P5.1-2

- **5.2-6** Given  $m(t) = \sin 2000\pi t$ ,  $k_f = 200,000\pi$ , and  $k_p = 10$ .
  - (a) Estimate the bandwidths of  $\varphi_{FM}(t)$  and  $\varphi_{PM}(t)$ .
  - (b) Repeat part (a) if the message signal amplitude is doubled.
  - (c) Repeat part (a) if the message signal frequency is doubled.
  - (d) Comment on the sensitivity of FM and PM bandwidths to the spectrum of m(t).

12°)

**5.4-2** A periodic square wave m(t) (Fig. P5.4-2a) frequency-modulates a carrier of frequency  $f_c=10$  kHz with  $\Delta f=1$  kHz. The carrier amplitude is A. The resulting FM signal is demodulated, as shown in Fig. P5.4-2b by the method discussed in Sec. 5.4 (Fig. 5.11). Sketch the waveforms at points b, c, d, and e.

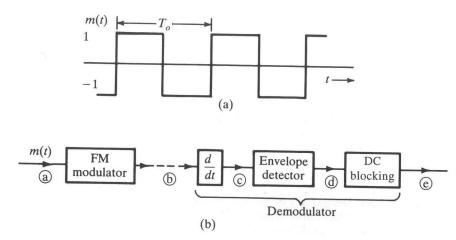


Figure P5.4-2

13°)

**6.1-6** A zero-order hold circuit (Fig. P6.1-6) is often used to reconstruct a signal g(t) from its samples.

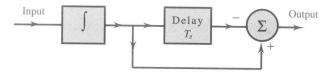


Figure P6.1-6

- (a) Find the unit impulse response of this circuit.
- (b) Find the transfer function  $H(\omega)$  and sketch  $|H(\omega)|$ .
- (c) Show that when a sampled signal  $\overline{g}(t)$  is applied at the input of this circuit, the output is a staircase approximation of g(t). The sampling interval is  $T_s$ .

- 6.2-2 A compact disc (CD) records audio signals digitally by using PCM. Assume the audio signal bandwidth to be 15 kHz.
  - (a) What is the Nyquist rate?
  - (b) If the Nyquist samples are quantized into L=65, 536 levels and then binary coded, determine the number of binary digits required to encode a sample.
  - (c) Determine the number of binary digits per second (bit/s) required to encode the audio signal.
  - (d) For practical reasons discussed in the text, signals are sampled at a rate well above the Nyquist rate. Practical CDs use 44,100 samples per second. If L=65,536, determine the number of bits per second required to encode the signal, and the minimum bandwidth required to transmit the encoded signal.
- **6.2-3** A television signal (video and audio) has a bandwidth of 4.5 MHz. This signal is sampled, quantized, and binary coded to obtain a PCM signal.
  - (a) Determine the sampling rate if the signal is to be sampled at a rate 20% above the Nyquist rate.
  - (b) If the samples are quantized into 1024 levels, determine the number of binary pulses required to encode each sample.
  - (c) Determine the binary pulse rate (bits per second) of the binary-coded signal, and the minimum bandwidth required to transmit this signal.

16°)

- **7.3-4** The Fourier transform  $P(\omega)$  of the basic pulse p(t) used in a certain binary communication system is shown in Fig. P7.3-4.
  - (a) From the shape of  $P(\omega)$ , explain if this pulse satisfies the Nyquist criterion.
  - (b) Find p(t) and verify that this pulse does (or does not) satisfy the Nyquist criterion.
  - (c) If the pulse does satisfy the Nyquist criterion, what is the transmission rate (in bits per second) and what is the roll-off factor?

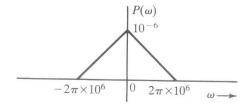


Figure P7.3-4

17°)

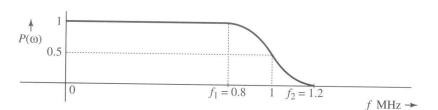


Figure P7.3-5

**7.3-6** Binary data at a rate of 1 Mbit/s is to be transmitted using Nyquist criterion pulses with  $P(\omega)$  shown in Fig. P7.3-5. The frequencies  $f_1$  and  $f_2$  (in hertz) of this spectrum are adjustable. The channel available for the transmission of this data has a bandwidth of 700 kHz. Determine  $f_1$  and  $f_2$  and the roll-off factor.

18°)

- **7.7-1** In multiamplitude scheme with M = 16,
  - (a) Determine the minimum transmission bandwidth required to transmit data at a rate of 12,000 bit/s with zero ISI.
  - (b) Determine the transmission bandwidth if Nyquist criterion pulses with a roll-off factor r=0.2 are used to transmit data.

19°)

- **7.7-3** Binary data is transmitted over a certain channel at a rate of  $R_b$  bit/s. To reduce the transmission bandwidth, it is decided to transmit this data using 8-ary multiamplitude signaling.
  - (a) By what factor is the bandwidth reduced?
  - (b) By what factor is the transmitted power increased, assuming the minimum separation between pulse amplitudes to be the same in both cases? *Hint:* Take the pulse amplitudes to be  $\pm A/2$ ,  $\pm 3A/2$ ,  $\pm 5A/2$ , and  $\pm 7A/2$  so that the minimum separation between various amplitude levels is A (the same as in the binary case pulses  $\pm A/2$ ). Assume all the eight levels equally likely.